

Physics 221A, Fall 2003

Course Outline

Instructor: Martin White, 561-C Campbell

GSI: Peter Shepard (pgs@socrates)

Lectures: M/W/F 9-10am, 102 Moffitt

Office Hours-MW: W 10-11 (561-C Campbell)

Office Hours-PS: M 11-12, F 1-2 (254 LeConte)

Section: T 4-5 (9 Evans), F 3-4 (71 Evans)

Exams: problem sets (30%), midterm (30%), final (40%)

Texts: Merzbacher (Sakurai, Baym, Liboff)

1. Fundamentals of Quantum Mechanics

- (a) Interference and uncertainty
- (b) Linear algebra, Hilbert spaces and bra-ket notation, connection with wave mechanics
- (c) Postulates of QM, precise statement of Uncertainty Principle
- (d) Polarized light and the density matrix
- (e) Entangled states, no-cloning theorem, EPR and Bell's inequalities
- (f) Quantum cryptography
- (g) Time evolution and the Schrödinger equation.
- (h) Schrödinger and Heisenberg pictures, spin precession and the non-classicality of the spin-vector
- (i) Connection with classical mechanics, Ehrenfest and virial theorems.
- (j) Path integral formulation.
- (k) Galilean invariance, wave packets and propagators
- (l) The Aharonov-Bohm effect

2. One-dimensional problems in Wave Mechanics

- (a) Connection of bra-ket notation with Wave Mechanics, stationary states
- (b) Conservation of probability current and spreading of the wavepacket
- (c) Escape proof box, bound states, symmetry of states, double well
- (d) Scattering theory in 1D, phase shift, resonances and bound states, evolution of a wave packet
- (e) Periodic potentials, Bloch waves and energy bands, tight binding model, and conductors, scattering off defects
- (f) Nanocircuits and the Quantum Point Contact, Landauer conductance
- (g) Harmonic oscillator, raising and lowering operators, coherent states
- (h) Example of decoherence, Schrödinger's cat

3. Interlude – Quantum computing

- (a) Qubits, gates and complexity
- (b) Single qubit logic gates
- (c) Finding the period of a sequence
- (d) Shor's factoring algorithm
- (e) Grover's search algorithm

4. WKB Methods

- (a) The classical limit and semi-classical methods
- (b) Matching conditions and integral quantization condition
- (c) Quantum bouncing ball and evanescent waves
- (d) Barrier penetration
- (e) WKB and the virial theorem

5. Angular Momentum

- (a) Group theory of rotations and angular momentum as generators
 - (b) Representations of the rotation group
 - (c) Vector addition coefficients
6. Many particles and many dimensions
- (a) Many particle systems
 - (b) Systems of more than 1D
7. Hydrogen atom
- (a) Central potentials
 - (b) Separation of variables
 - (c) Energy eigenvalues/eigenfunctions
 - (d) $O(4)$ symmetry
8. Time-independent perturbation theory
- (a) Rayleigh-Schrödinger non-degenerate perturbation theory
 - (b) Harmonic oscillator with a linear perturbation
 - (c) Degenerate perturbation theory
 - (d) Fine structure, Hyperfine structure, Zeeman effect, Stark effect, Van der Waals force
 - (e) Rayleigh-Ritz variational method
 - (f) Brillouin-Wigner expansion
9. Time-dependent perturbation theory
- (a) Interaction representation
 - (b) Transition rates
10. Scattering Theory
- (a) 3D scattering theory
 - (b) Elastic 2-body scattering
 - (c) Lifetimes of states